

# Embedded system paranoia: IAR Compiler with MPS430, (low power mixed signal RISC)

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## 1 Output results

Data kindly supplied by Jurg Stierli.

### 1.1 Fast Math libraries

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COMMENT: =====
COMMENT: Welcome to ESP - Embedded System Paranoia
COMMENT: Please let me know your experiences
COMMENT: and suggestions at lesh@oakcomp.co.uk or
COMMENT: L.Hatton@kent.ac.uk
COMMENT:
COMMENT: $Revision: 1.5 $ $Date: 2003/09/26 13:23:47 $
COMMENT: This version will attempt divide by zero.
COMMENT: This version uses <stdio.h>
COMMENT: This version uses <setjmp.h>
COMMENT: This version uses double precision.
COMMENT: =====
FAILURE: Comparison says -0.0 is non-zero !
COMMENT: Since comparison denies Z = 0, evaluating
COMMENT: (Z + Z) / Z should be safe.
COMMENT: This is a VERY SERIOUS DEFECT !
DEFECT : Z != Z * 1
COMMENT: Z = .17e, Z * 1 = .17e
DEFECT : Z != 1 * Z
COMMENT: Z = .17e, 1 * Z = .17e
DEFECT : Z != Z / 1
COMMENT: Z = .17e, Z / 1 = .17e
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-----> Diagnosis resuming after Milestone 0, Page 1

-----> Diagnosis resuming after Milestone 1, Page 2

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COMMENT: Searching for Radix and Precision.  
 COMMENT: Radix = .17e  
 COMMENT: Closest relative separation found is U1 = .17e  
 COMMENT: Recalculating radix and precision  
 COMMENT: confirms closest relative separation U1.  
 COMMENT: Radix confirmed.

-----> Diagnosis resuming after Milestone 10, Page 3

-----> Diagnosis resuming after Milestone 20, Page 4  
 COMMENT: The number of significant digits of the  
 COMMENT: Radix is .17e

-----> Diagnosis resuming after Milestone 25, Page 5

-----> Diagnosis resuming after Milestone 30, Page 6  
 COMMENT: Subtraction appears to be normalized, as it should be.  
 COMMENT: Checking for guard digit in \*, / and -.  
 PASSED : \*, /, and - appear to have guard digits, as they should.

-----> Diagnosis resuming after Milestone 35, Page 7  
 COMMENT: Checking rounding on multiply, divide and add/subtract.  
 PASSED : Multiplication appears to round correctly.

-----> Diagnosis resuming after Milestone 40, Page 8  
 FLAW : Division neither chopped nor correctly rounded.

-----> Diagnosis resuming after Milestone 45, Page 9  
 COMMENT: Addition/Subtraction neither rounds nor chops.  
 COMMENT: Sticky bit used incorrectly or not at all.  
 FLAW : Flaws are present due to lack of guard digits or round/chop failures

-----> Diagnosis resuming after Milestone 50, Page 10  
 COMMENT: Testing multiplicative commutation  
 COMMENT: with random pairs, trials = 20  
 PASSED : No failures found during these trials.

-----> Diagnosis resuming after Milestone 60, Page 11  
 COMMENT: Running test of square root(x).  
 FAILURE: Square root of 0.0, -0.0 or 1.0 wrong  
 COMMENT: Testing integer X,  $\text{sqrt}(X * X) = X$ , trials = 20  
 COMMENT: Test for sqrt monotonicity.  
 PASSED : sqrt has passed a test for Monotonicity.

-----> Diagnosis resuming after Milestone 70, Page 12  
 COMMENT: Running test of difference of two squares).  
 COMMENT: integer X,  $(X**2-Y**2) - (X-Y)(X+Y)$  trials = 20

-----> Diagnosis resuming after Milestone 75, Page 13

```

-----> Diagnosis resuming after Milestone 80, Page 14
COMMENT: Testing whether sqrt is rounded or chopped.
FLAW   : Square root is neither chopped nor correctly rounded.
COMMENT: Observed errors run from
COMMENT: .17e to .17e ulps.

-----> Diagnosis resuming after Milestone 85, Page 15

-----> Diagnosis resuming after Milestone 90, Page 16
COMMENT: Testing powers  $Z^i$  for small Integers Z and i.
DEFECT : Power function
COMMENT:  $.17e \wedge .17e = .17e$ 
COMMENT: which differs from correct value by .17e
COMMENT: Number of similar discrepancies = 3
DEFECT : Power function
COMMENT:  $.17e \wedge .17e = .17e$ 
COMMENT: which differs from correct value by .17e
COMMENT: Number of similar discrepancies = 1
DEFECT : Power function
COMMENT:  $.17e \wedge .17e = .17e$ 
COMMENT: which differs from correct value by .17e

-----> Diagnosis resuming after Milestone 91, Page 17
COMMENT: Errors like this may invalidate financial calculations
COMMENT: involving interest rates.
COMMENT: Number of similar discrepancies = 72

-----> Diagnosis resuming after Milestone 100, Page 18
COMMENT: Seeking Underflow thresholds UfThold and E0.

-----> Diagnosis resuming after Milestone 110, Page 19
COMMENT: Smallest strictly positive number found
COMMENT: is E0 = .17e
COMMENT: Since comparison denies  $Z = 0$ , evaluating
COMMENT:  $(Z + Z) / Z$  should be safe.
COMMENT:  $(Z+Z)/Z$  is OK provided Over/Underflow
COMMENT: has NOT just been signaled.

-----> Diagnosis resuming after Milestone 120, Page 20
FLAW   :
COMMENT:  $X \neq Z$  but  $X - Z = \text{Zero}$ 
COMMENT:  $X = .17e, Z = .17e$ 
COMMENT: This is OK only if underflow signalled.
COMMENT:  $X / Z = 1 + .17e$ 
COMMENT: The Underflow threshold is .17e
COMMENT: Below this, a calculation may suffer larger Relative
COMMENT: error than merely roundoff.

-----> Diagnosis resuming after Milestone 121, Page 21

```

COMMENT: Since underflow occurs below the threshold  
COMMENT: UfThold =  $.17e \wedge .17e$   
COMMENT: only underflow could affect this expression.  
COMMENT: calculating yields:  $.17e$   
PASSED : This computed value is O.K.

-----> Diagnosis resuming after Milestone 130, Page 22  
COMMENT: As  $X \rightarrow 1$ , Testing  $X^{\frac{X+1}{X-1}}$  against  $\exp(2)$ .  
COMMENT:  $\exp(2) = .17e$   
DEFECT : Power function  $\text{pow}(x,z)$ :  
COMMENT:  $(1 + .17e) \wedge .17e$   
COMMENT: differs from correct value by  $.17e$   
COMMENT: This may spoil financial calculations  
COMMENT: involving tiny interest rates.

-----> Diagnosis resuming after Milestone 140, Page 23  
COMMENT: Testing powers  $Z^Q$  at four nearly extreme values.

DEFECT : Power function  
COMMENT:  $.17e \wedge .17e = .17e$   
COMMENT: which differs from correct value by  $.17e$   
COMMENT: Number of similar discrepancies = 3

-----> Diagnosis resuming after Milestone 150, Page 24

-----> Diagnosis resuming after Milestone 160, Page 25  
COMMENT: Searching for Overflow threshold:  
COMMENT: This may generate an error.  
COMMENT: Can 'Z = -Y' overflow?  
COMMENT: Trying it on  $Y = .17e$   
PASSED : Seems O.K.  
COMMENT: Overflow threshold is  $V = .17e$   
COMMENT: Overflow saturates at  $V_0 = .17e$   
COMMENT: No overflow should be signalled for  $V*1 = .17e$   
COMMENT: No overflow should be signalled for  $V/1 = .17e$   
COMMENT: Any overflow separating  $V*1$  from  
COMMENT:  $V$  above is a DEFECT.

-----> Diagnosis resuming after Milestone 161, Page 26

-----> Diagnosis resuming after Milestone 170, Page 27

-----> Diagnosis resuming after Milestone 175, Page 28  
DEFECT :  
COMMENT: Comparison alleges that  $Z = .17e$   
COMMENT: is too far from  $\sqrt{Z} \wedge 2 = .17e$

-----> Diagnosis resuming after Milestone 180, Page 29

-----> Diagnosis resuming after Milestone 190, Page 30

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-----> Diagnosis resuming after Milestone 191, Page 31

-----> Diagnosis resuming after Milestone 200, Page 32
COMMENT: Trying to compute 1/0 gives .17e
COMMENT: Trying to compute 0/0 gives .17e

-----> Diagnosis resuming after Milestone 210, Page 33
COMMENT: =====
COMMENT:      Embedded System Paranoia SUMMARY
COMMENT:
COMMENT: Number of FAILURES encountered      = 2
COMMENT: Number of SERIOUS DEFECTs discovered = 1
COMMENT: Number of DEFECTs discovered         = 9
COMMENT: Number of FLAWs discovered          = 4
COMMENT:
FAILED : The arithmetic diagnosed has unacceptable
COMMENT: Serious DEFECT.
FAILED : Potentially fatal FAILURE has occurred
COMMENT:
COMMENT: Rating ...
COMMENT:
           Excellent
           Very good
           Good
           Acceptable
           Unacceptable
=====> Broken
COMMENT:
COMMENT: END OF TEST.
COMMENT: =====

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## 1.2 IEEElibrary

```

COMMENT: =====
COMMENT: Welcome to ESP - Embedded System Paranoia
COMMENT: Please let me know your experiences
COMMENT: and suggestions at lesh@oakcomp.co.uk or
COMMENT: L.Hatton@kent.ac.uk
COMMENT:
COMMENT: $Revision: 1.5 $ $Date: 2003/09/26 13:23:47 $
COMMENT: This version will attempt divide by zero.
COMMENT: This version uses <stdio.h>
COMMENT: This version uses <setjmp.h>
COMMENT: This version uses double precision.
COMMENT: =====

-----> Diagnosis resuming after Milestone 0, Page 1
COMMENT: -1, 0, 1/2, 1, 2, 3, 4, 5, 9, 27, 32 & 240
PASSED : small integer tests are all OK.

```

COMMENT: Searching for Radix and Precision.  
 COMMENT: Radix = .17e  
 COMMENT: Closest relative separation found is U1 = .17e  
 COMMENT: Recalculating radix and precision  
 COMMENT: confirms closest relative separation U1.  
 COMMENT: Radix confirmed.

-----> Diagnosis resuming after Milestone 10, Page 2

-----> Diagnosis resuming after Milestone 20, Page 3  
 COMMENT: The number of significant digits of the  
 COMMENT: Radix is .17e

-----> Diagnosis resuming after Milestone 25, Page 4

-----> Diagnosis resuming after Milestone 30, Page 5  
 COMMENT: Subtraction appears to be normalized, as it should be.  
 COMMENT: Checking for guard digit in \*, / and -.  
 PASSED : \*, /, and - appear to have guard digits, as they should.

-----> Diagnosis resuming after Milestone 35, Page 6  
 COMMENT: Checking rounding on multiply, divide and add/subtract.  
 PASSED : Multiplication appears to round correctly.

-----> Diagnosis resuming after Milestone 40, Page 7  
 PASSED : Division appears to round correctly.

-----> Diagnosis resuming after Milestone 45, Page 8  
 PASSED : Addition/Subtraction appears to round correctly.  
 COMMENT: Checking for sticky bit.

PASSED : Sticky bit apparently used correctly.

-----> Diagnosis resuming after Milestone 50, Page 9  
 COMMENT: Testing multiplicative commutation  
 COMMENT: with random pairs, trials = 20  
 PASSED : No failures found during these trials.

-----> Diagnosis resuming after Milestone 60, Page 10  
 COMMENT: Running test of square root(x).  
 COMMENT: Testing integer X,  $\text{sqrt}(X * X) = X$ , trials = 20  
 COMMENT: Test for sqrt monotonicity.  
 PASSED : sqrt has passed a test for Monotonicity.

-----> Diagnosis resuming after Milestone 70, Page 11  
 COMMENT: Running test of difference of two squares).  
 COMMENT: integer X,  $(X**2-Y**2) - (X-Y)(X+Y)$  trials = 20

-----> Diagnosis resuming after Milestone 75, Page 12

```

-----> Diagnosis resuming after Milestone 80, Page 13
COMMENT: Testing whether sqrt is rounded or chopped.
FLAW  : Square root is neither chopped nor correctly rounded.
COMMENT: Observed errors run from
COMMENT: .17e to .17e ulps.

-----> Diagnosis resuming after Milestone 85, Page 14

-----> Diagnosis resuming after Milestone 90, Page 15
COMMENT: Testing powers  $Z^i$  for small Integers Z and i.
DEFECT : Power function
COMMENT:  $.17e \wedge .17e = .17e$ 
COMMENT: which differs from correct value by .17e
COMMENT: Number of similar discrepancies = 1
DEFECT : Power function
COMMENT:  $.17e \wedge .17e = .17e$ 
COMMENT: which differs from correct value by .17e

-----> Diagnosis resuming after Milestone 91, Page 16
COMMENT: Errors like this may invalidate financial calculations
COMMENT: involving interest rates.
COMMENT: Number of similar discrepancies = 81

-----> Diagnosis resuming after Milestone 100, Page 17
COMMENT: Seeking Underflow thresholds UfThold and E0.

-----> Diagnosis resuming after Milestone 110, Page 18
COMMENT: Smallest strictly positive number found
COMMENT: is E0 = .17e
COMMENT: Since comparison denies  $Z = 0$ , evaluating
COMMENT:  $(Z + Z) / Z$  should be safe.
COMMENT:  $(Z+Z)/Z$  is OK provided Over/Underflow
COMMENT: has NOT just been signaled.

COMMENT: Underflow is gradual; Absolute roundoff error in  $UfThold < E0$ .
COMMENT: The Underflow threshold is .17e
COMMENT: Below this, a calculation may suffer larger Relative
COMMENT: error than merely roundoff.

-----> Diagnosis resuming after Milestone 120, Page 19
COMMENT: Since underflow occurs below the threshold
COMMENT:  $UfThold = .17e \wedge .17e$ 
COMMENT: only underflow could affect this expression.
COMMENT: calculating yields: .17e
PASSED : This computed value is O.K.

-----> Diagnosis resuming after Milestone 130, Page 20
COMMENT: As  $X \rightarrow 1$ , Testing  $X^{((X + 1) / (X - 1))}$  against  $\exp(2)$ .
COMMENT:  $\exp(2) = .17e$ 
DEFECT : Power function  $\text{pow}(x,z)$ :

```

COMMENT:  $(1 + .17e)^{.17e}$   
 COMMENT: differs from correct value by  $.17e$   
 COMMENT: This may spoil financial calculations  
 COMMENT: involving tiny interest rates.

-----> Diagnosis resuming after Milestone 140, Page 21  
 COMMENT: Testing powers  $Z^Q$  at four nearly extreme values.

DEFECT : Power function  
 COMMENT:  $.17e^{.17e} = .17e$   
 COMMENT: which differs from correct value by  $.17e$   
 COMMENT: Number of similar discrepancies = 4

-----> Diagnosis resuming after Milestone 150, Page 22

-----> Diagnosis resuming after Milestone 160, Page 23  
 COMMENT: Searching for Overflow threshold:  
 COMMENT: This may generate an error.  
 COMMENT: Can 'Z = -Y' overflow?  
 COMMENT: Trying it on  $Y = .17e$   
 PASSED : Seems O.K.  
 COMMENT: Overflow threshold is  $V = .17e$   
 COMMENT: Overflow saturates at  $V_0 = .17e$   
 COMMENT: No overflow should be signalled for  $V*1 = .17e$   
 COMMENT: No overflow should be signalled for  $V/1 = .17e$   
 COMMENT: Any overflow separating  $V*1$  from  
 COMMENT:  $V$  above is a DEFECT.

-----> Diagnosis resuming after Milestone 161, Page 24

-----> Diagnosis resuming after Milestone 170, Page 25  
 DEFECT :  
 COMMENT: Comparison alleges that what prints as  $Z = .17e$   
 COMMENT: is too far from  $.17e$

-----> Diagnosis resuming after Milestone 175, Page 26  
 DEFECT :  
 COMMENT: Comparison alleges that  $Z = .17e$   
 COMMENT: is too far from  $\sqrt{Z}^2 = .17e$

-----> Diagnosis resuming after Milestone 180, Page 27

-----> Diagnosis resuming after Milestone 190, Page 28

-----> Diagnosis resuming after Milestone 191, Page 29

-----> Diagnosis resuming after Milestone 200, Page 30  
 COMMENT: Trying to compute  $1/0$  gives  $.17e$   
 COMMENT: Trying to compute  $0/0$  gives  $.17e$



```

-----> Diagnosis resuming after Milestone 210, Page 31
COMMENT: =====
COMMENT:      Embedded System Paranoia SUMMARY
COMMENT:
COMMENT: Number of FAILURES encountered      = 0
COMMENT: Number of SERIOUS DEFECTs discovered = 0
COMMENT: Number of DEFECTs discovered        = 6
COMMENT: Number of FLAWs discovered          = 1
COMMENT:
COMMENT: The arithmetic diagnosed may be Acceptable
COMMENT: despite inconvenient DEFECT.
COMMENT:
COMMENT: Rating ...
COMMENT:
          Excellent
          Very good
          Good
=====> Acceptable
          Unacceptable
          Broken
COMMENT:
COMMENT: END OF TEST.
COMMENT: =====

```

### 1.3 EC++ library

```

COMMENT: =====
COMMENT: Welcome to ESP - Embedded System Paranoia
COMMENT: Please let me know your experiences
COMMENT: and suggestions at lesh@oakcomp.co.uk or
COMMENT: L.Hatton@kent.ac.uk
COMMENT:
COMMENT: $Revision: 1.5 $ $Date: 2003/09/26 13:23:47 $
COMMENT: This version will attempt divide by zero.
COMMENT: This version uses <stdio.h>
COMMENT: This version uses <setjmp.h>
COMMENT: This version uses double precision.
COMMENT: =====

```

```

-----> Diagnosis resuming after Milestone 0, Page 1
COMMENT: -1, 0, 1/2, 1, 2, 3, 4, 5, 9, 27, 32 & 240
PASSED : small integer tests are all OK.
COMMENT: Searching for Radix and Precision.
COMMENT: Radix = 2.0000000000000000e+00
COMMENT: Closest relative separation found is U1 = 5.9604000000000000e-08
COMMENT: Recalculating radix and precision
COMMENT: confirms closest relative separation U1.
COMMENT: Radix confirmed.

```

```

-----> Diagnosis resuming after Milestone 10, Page 2

```

```

-----> Diagnosis resuming after Milestone 20, Page 3
COMMENT: The number of significant digits of the
COMMENT: Radix is 2.4000000000000000e+01

-----> Diagnosis resuming after Milestone 25, Page 4

-----> Diagnosis resuming after Milestone 30, Page 5
COMMENT: Subtraction appears to be normalized, as it should be.
COMMENT: Checking for guard digit in *, / and -.
PASSED : *, /, and - appear to have guard digits, as they should.

-----> Diagnosis resuming after Milestone 35, Page 6
COMMENT: Checking rounding on multiply, divide and add/subtract.
PASSED : Multiplication appears to round correctly.

-----> Diagnosis resuming after Milestone 40, Page 7
PASSED : Division appears to round correctly.

-----> Diagnosis resuming after Milestone 45, Page 8
PASSED : Addition/Subtraction appears to round correctly.
COMMENT: Checking for sticky bit.

PASSED : Sticky bit apparently used correctly.

-----> Diagnosis resuming after Milestone 50, Page 9
COMMENT: Testing multiplicative commutation
COMMENT: with random pairs, trials = 20
PASSED : No failures found during these trials.

-----> Diagnosis resuming after Milestone 60, Page 10
COMMENT: Running test of square root(x).
COMMENT: Testing integer X, sqrt(X * X) = X, trials = 20
COMMENT: Test for sqrt monotonicity.
PASSED : sqrt has passed a test for Monotonicity.

-----> Diagnosis resuming after Milestone 70, Page 11
COMMENT: Running test of difference of two squares).
COMMENT: integer X, (X**2-Y**2) - (X-Y)(X+Y) trials = 20

-----> Diagnosis resuming after Milestone 75, Page 12

-----> Diagnosis resuming after Milestone 80, Page 13
COMMENT: Testing whether sqrt is rounded or chopped.
FLAW  : Square root is neither chopped nor correctly rounded.
COMMENT: Observed errors run from
COMMENT: -5.0000000000000000e-01 to 5.0000000000000000e-01 ulps.

-----> Diagnosis resuming after Milestone 85, Page 14

```

```

-----> Diagnosis resuming after Milestone 90, Page 15
COMMENT: Testing powers  $Z^i$  for small Integers Z and i.
COMMENT: Power function
COMMENT:  $-0.0000000000000000e+00 \wedge 0.0000000000000000e+00 = -NaN$ 
COMMENT: which differs from correct value by  $-NaN$ 
COMMENT: Number of similar discrepancies = 1

-----> Diagnosis resuming after Milestone 91, Page 16
PASSED : ... no discrepancies found.

-----> Diagnosis resuming after Milestone 100, Page 17
COMMENT: Seeking Underflow thresholds UfThold and E0.

-----> Diagnosis resuming after Milestone 110, Page 18
COMMENT: Smallest strictly positive number found
COMMENT: is E0 =  $1.4012900000000000e-45$ 
COMMENT: Since comparison denies  $Z = 0$ , evaluating
COMMENT:  $(Z + Z) / Z$  should be safe.
COMMENT:  $(Z+Z)/Z$  is OK provided Over/Underflow
COMMENT: has NOT just been signaled.

COMMENT: Underflow is gradual; Absolute roundoff error in UfThold < E0.
COMMENT: The Underflow threshold is  $1.1754940000000000e-38$ 
COMMENT: Below this, a calculation may suffer larger Relative
COMMENT: error than merely roundoff.

-----> Diagnosis resuming after Milestone 120, Page 19
COMMENT: Since underflow occurs below the threshold
COMMENT: UfThold =  $2.0000000000000000e+00 \wedge -1.2600000000000000e+02$ 
COMMENT: only underflow could affect this expression.
COMMENT: calculating yields:  $0.0000000000000000e+00$ 
PASSED : This computed value is O.K.

-----> Diagnosis resuming after Milestone 130, Page 20
COMMENT: As  $X \rightarrow 1$ , Testing  $X^{((X + 1) / (X - 1))}$  against  $\exp(2)$ .
COMMENT:  $\exp(2) = 7.3890550000000000e+00$ 
PASSED : Accuracy seems adequate.

-----> Diagnosis resuming after Milestone 140, Page 21
COMMENT: Testing powers  $Z^Q$  at four nearly extreme values.

PASSED : ... no discrepancies found.

-----> Diagnosis resuming after Milestone 150, Page 22

-----> Diagnosis resuming after Milestone 160, Page 23
COMMENT: Searching for Overflow threshold:
COMMENT: This may generate an error.
COMMENT: Can 'Z = -Y' overflow?
COMMENT: Trying it on  $Y = -Inf$ 

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```

PASSED : Seems O.K.
COMMENT: Overflow threshold is V = 3.4028230000000000e+38
COMMENT: Overflow saturates at V0 = Inf
COMMENT: No overflow should be signalled for V*1 = 3.4028230000000000e+38
COMMENT: No overflow should be signalled for V/1 = 3.4028230000000000e+38
COMMENT: Any overflow separating V*1 from
COMMENT: V above is a DEFECT.

-----> Diagnosis resuming after Milestone 161, Page 24

-----> Diagnosis resuming after Milestone 170, Page 25

-----> Diagnosis resuming after Milestone 175, Page 26

-----> Diagnosis resuming after Milestone 180, Page 27

-----> Diagnosis resuming after Milestone 190, Page 28

-----> Diagnosis resuming after Milestone 191, Page 29

-----> Diagnosis resuming after Milestone 200, Page 30
COMMENT: Trying to compute 1/0 gives Inf
COMMENT: Trying to compute 0/0 gives NaN

-----> Diagnosis resuming after Milestone 210, Page 31
COMMENT: =====
COMMENT:      Embedded System Paranoia SUMMARY
COMMENT:
COMMENT: Number of FAILURES encountered      = 0
COMMENT: Number of SERIOUS DEFECTs discovered = 0
COMMENT: Number of DEFECTs discovered         = 0
COMMENT: Number of FLAWs discovered           = 1
COMMENT:
PASSED : The arithmetic diagnosed seems satisfactory
COMMENT: though flawed.
COMMENT:
COMMENT: Rating ...
COMMENT:
           Excellent
           Very good
=====> Good
           Acceptable
           Unacceptable
           Broken

COMMENT:
COMMENT: END OF TEST.
COMMENT: =====

```